# Study Guide and Intervention (continued)

## Angles and Arcs

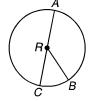
Arc Length An arc is part of a circle and its length is a part of the circumference of the circle.

## Example

In  $\bigcirc R$ ,  $m \angle ARB = 135$ , RB = 8, and

AC is a diameter. Find the length of  $\widehat{AB}$ .

 $m\angle ARB = 135$ , so  $m\overrightarrow{AB} = 135$ . Using the formula  $C = 2\pi r$ , the circumference is  $2\pi(8)$  or  $16\pi$ . To find the length of  $\widehat{AB}$ , write a proportion to compare each part to its whole.



$$\frac{\text{length of } \widehat{AB}}{\text{circumference}} = \frac{\text{degree measure of arc}}{\text{degree measure of circle}} \qquad \text{Proportion}$$
 
$$\frac{\ell}{16\pi} = \frac{135}{360} \qquad \qquad \text{Substitution}$$
 
$$\ell = \frac{(16\pi)(135)}{360} \qquad \qquad \text{Multiply each}$$

Multiply each side by  $16\pi$ . 360

The length of  $\widehat{AB}$  is  $6\pi$  or about 18.85 units.

### Exercises

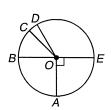
The diameter of  $\odot O$  is 24 units long. Find the length of each arc for the given angle measure.

**1.** 
$$\widehat{DE}$$
 if  $m \angle DOE = 120$ 

**2.** 
$$\widehat{DEA}$$
 if  $m \angle DOE = 120$ 

**3.** 
$$\widehat{BC}$$
 if  $m \angle COB = 45$ 

**4.** 
$$\widehat{CBA}$$
 if  $m \angle COB = 45$ 



The diameter of  $\bigcirc P$  is 15 units long and  $\angle SPT \cong \angle RPT$ . Find the length of each arc for the given angle measure.

**5.** 
$$\widehat{RT}$$
 if  $m \angle SPT = 70$ 

**6.** 
$$\widehat{NR}$$
 if  $m \angle RPT = 50$ 

7. 
$$\widehat{MST}$$

**8.** 
$$\widehat{MRS}$$
 if  $m \angle MPS = 140$ 

