Study Guide and Intervention (continued)

Exponential Growth and Decay

Exponential Growth Population increase and growth of bacteria colonies are examples of exponential growth. When a quantity increases by a fixed percent each time period, the amount of that quantity after t time periods is given by $y = a(1 + r)^t$, where a is the initial amount and r is the percent increase (or rate of growth) expressed as a decimal. Another exponential growth model often used by scientists is $y = ae^{kt}$, where k is a constant.

Example A computer engineer is hired for a salary of \$28,000. If she gets a 5% raise each year, after how many years will she be making \$50,000 or more? Use the exponential growth model with a = 28,000, y = 50,000, and r = 0.05 and solve for t.

$$y=a(1+r)^t$$
 Exponential growth formula $50,000=28,000(1+0.05)^t$ $y=50,000, a=28,000, r=0.05$ $\frac{50}{28}=(1.05)^t$ Divide each side by 28,000. $\log\left(\frac{50}{28}\right)=\log\left(1.05\right)^t$ Property of Equality of Logarithms $\log\left(\frac{50}{28}\right)=t\log 1.05$ Power Property $t=\frac{\log\left(\frac{50}{28}\right)}{\log 1.05}$ Divide each side by $t=1.9$ years Use a calculator.

If raises are given annually, she will be making over \$50,000 in 12 years.

Exercises

- 1. BACTERIA GROWTH A certain strain of bacteria grows from 40 to 326 in 120 minutes. Find k for the growth formula $y = ae^{kt}$, where t is in minutes.
- 2. INVESTMENT Carl plans to invest \$500 at 8.25% interest, compounded continuously. How long will it take for his money to triple?
- **3. SCHOOL POPULATION** There are currently 850 students at the high school, which represents full capacity. The town plans an addition to house 400 more students. If the school population grows at 7.8% per year, in how many years will the new addition be full?
- **4. EXERCISE** Hugo begins a walking program by walking $\frac{1}{2}$ mile per day for one week. Each week thereafter he increases his mileage by 10%. After how many weeks is he walking more than 5 miles per day?
- 5. VOCABULARY GROWTH When Emily was 18 months old, she had a 10-word vocabulary. By the time she was 5 years old (60 months), her vocabulary was 2500 words. If her vocabulary increased at a constant percent per month, what was that increase?