

**9-4 Study Guide and Intervention** *(continued)***Common Logarithms**

**Change of Base Formula** The following formula is used to change expressions with different logarithmic bases to common logarithm expressions.

**Change of Base Formula**For all positive numbers  $a$ ,  $b$ , and  $n$ , where  $a \neq 1$  and  $b \neq 1$ ,  $\log_a n = \frac{\log_b n}{\log_b a}$ **Example**

Express  $\log_8 15$  in terms of common logarithms. Then approximate its value to four decimal places.

$$\log_8 15 = \frac{\log_{10} 15}{\log_{10} 8} \quad \text{Change of Base Formula}$$

$$\approx 1.3023 \quad \text{Simplify.}$$

The value of  $\log_8 15$  is approximately 1.3023.

**Exercises**

Express each logarithm in terms of common logarithms. Then approximate its value to four decimal places.

1.  $\log_3 16$

2.  $\log_2 40$

3.  $\log_5 35$

4.  $\log_4 22$

5.  $\log_{12} 200$

6.  $\log_2 50$

7.  $\log_5 0.4$

8.  $\log_3 2$

9.  $\log_4 28.5$

10.  $\log_3 (20)^2$

11.  $\log_6 (5)^4$

12.  $\log_8 (4)^5$

13.  $\log_5 (8)^3$

14.  $\log_2 (3.6)^6$

15.  $\log_{12} (10.5)^4$

16.  $\log_3 \sqrt{150}$

17.  $\log_4 \sqrt[3]{39}$

18.  $\log_5 \sqrt[4]{1600}$