In Exercises 1–4, solve the equation.

1.
$$q^3 - q^2 - 30q = 0$$
 2. $k^3 + 6k^2 + 9k = 0$

3.
$$3y^4 - 6y^3 = -3y^2$$

4. $n^3 + 2n^2 - 9n - 18 = 0$

In Exercises 5–10, find the zeros of the function.

5.

$$f(x) = x^4 + x^3 - 12x^2$$
 6. $g(x) = x^4 - 8x^2 + 16$

7.
$$f(x) = x^4 - 8x^2 - 9$$

8. $f(x) = x^4 - 5x^2 - 36$

9.
$$g(x) = x^3 + 2x^2 - 5x - 6$$

10. $f(x) = x^4 - 5x^3 + 7x^2 + 3x - 10$

In Exercises 11–13, write a polynomial function f of least degree that has rational coefficients, a leading coefficient of 1, and the given zeros.

11. -4, 1, 2 **12.** 3,
$$-\sqrt{7}$$
 13. 2, 3 + *i*

In Exercises 14-17, describe the transformation of f represented by g.

14.
$$f(x) = x^3$$
, $g(x) = x^3 - 2$
15. $f(x) = x^3$, $g(x) = (x+3)^3$

16.
$$f(x) = x^4$$
, $g(x) = -5x^4$
17. $f(x) = x^3$, $g(x) = 4x^3 - 3$

In Exercises 18-21, write a rule for g and describe the graph of g as a transformation of the graph of f. 18. $f(x) = x^3 + 2$, g(x) = f(x - 1)19. $f(x) = x^4 - 3x + 1$, g(x) = 2f(x)

20.
$$f(x) = x^3 - 4x^2 + 2$$
, $g(x) = -\frac{1}{4}f(x)$
21. $f(x) = x^4 + x + 1$, $g(x) = f(-x) + 2$

In Exercises 22 - 24, write a rule for *g* that represents the indicated transformations of the graph of *f*. 22. $f(x) = x^3 + 5$; translation 2 units right, followed by a reflection in the *x*-axis

23. $f(x) = x^4 - 3x + 1$; vertical shrink by a factor of $\frac{1}{3}$, followed by a translation 2 units down

24. $f(x) = x^3 - 3x^2 + 2$; reflection in the y-axis and a horizontal stretch by a factor of 3, followed by a translation 3 units up

In Exercises 25 and 26, graph the function.





In Exercises 27 and 28, sketch the graph of a function with the given characteristics.

27. Degree 4 polynomial with 4 distinct real roots.



28. Degree 3 polynomial with a single real root and a double real root.



In Exercises 29 and 30, determine whether each function is even, odd, or neither. 29. $f(x) = x^3 - 8x^2 + 15x$ 30. $f(x) = x^4 + 5x^2 - 8$

31. Use the graph to identify the x-intercepts, the local max, local min, the intervals where the function is increasing, and the intervals where the function is decreasing.



In Exercises 32 and 33, write a cubic function whose graph passes through the given points.



33.

